

List of Topics

1. First presentation(September 17) :

- Half-plane model (All)
- Hyperbolic length and hyperbolic lines in the half-plane([A], [CFKP], [W])
- Poincaré disc model (All but [K])
- Hyperbolic length and hyperbolic lines in the Poincaré disc ([A], [CFKP],[W, Section 6])
- Hyperboloid model ([BP],[CFKP])
- Hyperbolic length in the hyperboloid model ([BP],[CFKP])
- Connection among these models.
- [Hyperbolic distance](#) ([A], [W, Section 2])
- Optional : Other models

2. Second presentation(September 24)

- Möbius transformation on the half-plane(All but [CFKP])
- [Möbius transformations form a group](#)([A],[S],[W])
- [Möbius transformation is an isometry](#) ([A],[S],[W])
- [Möbius transformation on the Poincaré disc](#) ([A],[S],[W])
- Transitivity of Möbius transformation ([A, Chapter 2],[S], [W])
- Möbius transformation maps any hyperbolic lines to any hyperbolic lines ([A],[S],[W])
- Geodesic = Hyperbolic line ([A],[S], [W])
- Euclid's parallel postulate fails

3. Third presentation(October 8)

- Formula for hyperbolic distance in half-plane([A], [S], [W])
- Formula for hyperbolic distance in Poincaré disc ([A], [S],[W])
- Möbius transformation = Isometry of hyperbolic plane ([A, Section 3.6],[S])
- Conformality of Möbius transformation ([A],[S], [W])
- Pythagoras' theorem for hyperbolic space ([A], [S],[W])
- Optional : Hyperbolic trigonometry ([A],[S],[W])

4. Fourth presentation(October 15)

- [Hyperbolic area](#) ([A],[S],[W])
- [Möbius transformation preserves hyperbolic area](#)([A], [S], [W])

- Classification of Möbius transformation with the number of fixed points(All but [BP], [CFKP])
- Classification of Möbius transformation with trace (All but [BP],[CFKP])
- Conjugacy([A],[S],[W])
- Every Möbius transformation on the hyperbolic plane is conjugate to either a translation, a dilation in the half-plane model or a rotation in the Poincare disc model.([W])